## GENERAL MATHS NETWORKS APPLICATION TASK

## NAME:

A diagram of the senior courtyard is shown below, with vertices labeled with dots and named.



1.

a. How many vertices are there in this diagram? \_\_\_\_

- **b.** If a graph is drawn in the courtyard and each of the garden beds is a face, how many faces are there? Add these to the diagram above.
- **2.** Assuming that Euler's law holds for a network drawn in the senior courtyard, how many edges will there be in a connected planar graph with this many faces and vertices.

**3.** Add this number of edges to the diagram above. Can you make a connected planar graph with the vertices positioned as they are? If not draw an isomorphic graph meeting all criteria.

**4.** The adjacency matrix for a different graph is shown below. Using this matrix draw the graph.



## 5.

**a.** This graph will have an Eulerian trail but not an Eulerian circuit. Explain why with reference to the degrees of vertices and identify this trail.

**b.** Will this graph have an Hamiltonian path, Hamiltonian cycle or neither? Explain your answer with reference to the degrees of vertices.

- **c.** Add the number of steps required to walk each edge of the graph you have drawn to the diagram above.
- **6.** Identify the minimum spanning tree for this graph using a different colour above and calculate the minimum number of steps required to visit all the vertices in the senior courtyard.